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# Blood flow velocity effects and role of activation delay time on growth and form of platelet thrombi

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**Mural thrombi are composed dominantly of platelets and develop under a blood flow. Portions can break off and are carried in the blood flow as emboli. Thrombus growth rates are affected by the velocity of the blood flow, but they do not simply increase with it, they exhibit a maximum, with subsequent decrease. Whereas this variation indicates an interaction of biochemical and physical processes, studies have concentrated widely on understanding only the biochemical processes. Here we show results of simulation of thrombus formation in 3D flows by accounting for the movements of individual platelets. Each platelet follows prescribed rules for interactions while the local flow around the thrombus continuously adjusts to the growing structure of the thrombus, also when embolization occurs. With an activation delay time assigned to each platelet we demonstrate the dependence of thrombus growth rate on blood velocity as found experimentally by Begent and Born [Begent N, Born GV (1970) *Nature* 227:926–930]. With activated platelets having mutual tensile action sustainable up to a prescribed distance we achieve thrombus growth faster than with shorter maximum distances that make a thrombus less porous; when the prescribed maximum distance is large enough the thrombus shape is not like a “hill” but like a “carpet.” We find that thrombus growth rate is enhanced by modest pulsatility but less so when pulsations are amplified in part because of more embolization.**

direct numerical simulations | platelet aggregation | *in vivo* comparison | stochastic modeling

**A**cute thrombogenesis in a flowing bloodstream can occur on damaged tissues in normal circulation (1). It has also been observed in blood flow over vascular prostheses (2) and in artificial internal organs, such as prosthetic heart valves (3). The thrombi are composed predominantly of platelets, and they can develop even in the presence of systemic anticoagulants such as heparin (4).

Blood flow velocity effects were investigated systematically *in vivo* by Begent and Born (1), who obtained quantitative data on thrombus growth rates for a range of blood flow rates. Their study remains the clearest time-resolved *in vivo* study of the effect of blood flow rates on thrombus formation. Richardson (5) subsequently proposed that Begent and Born's observations were consistent with a shear-flow aggregation process (6, 7) in which an activation delay time of the platelets is allowed for, a delay time between each platelet's close encounter with the thrombus and its development of ability to adhere to the thrombus, and which was estimated then to be the order of 0.1–0.2 s. A predicted consequence of this finding was that the height-to-length ratio for thrombi would be lower in blood flows, where a significant fraction of the activated platelets escaped the primary thrombus before their activation delay time had elapsed; this was demonstrated later by Born and Richardson (8). More recent experiments by Petrishchev and Mikhailova (9) *in vivo* and van Gestel *et al.* (10) *in vitro* produced qualitatively similar results as the ones of Begent and Born but they lack the quantitative details required for validating simulation results.

At the time of Begent and Born's studies there were handicaps to carrying the implications further. The biological handicap was the lack of specific knowledge of cell membrane channels and

receptors, and therefore of cell mechanics by which an activation delay time could be mediated (and varied). The computational handicap was that computing capability then available was inadequate to consider the movements of, say, 50,000 individual platelets in a blood flow where thrombus growth is initiated at one location on a wall. This latter handicap now has diminished, and this article describes what is found in running simulations of the Begent and Born flow situations and what can be predicted about thrombus formation in pulsatile flows. The latter is a circumstance important to clinical conditions such as thrombo-embolic stroke and myocardial infarction involving thrombus formation on fissured atherosclerotic plaques in carotid and coronary arteries.

## Numerical Simulations

Simulations representing 3D blood flow were performed for a 50- $\mu\text{m}$ -diameter straight tube, with 500- $\mu\text{m}$  length at several different steady blood flow rates. Platelets are considered uniformly distributed in the inflow, with the latter having a parabolic velocity profile at entry. The mean velocity distribution alters downstream, over time, as a thrombus forms on the wall and acts as an obstacle to the flow; there is an interaction between the flow and the structure formed by the thrombus. The time-dependent computations continuously update the geometry of the thrombus with regard both to size and shape. This procedure was followed for blood flow rates both below and above the rate, which is expected to provide the maximum relative rate of growth. This approach provided simulation results, which can be compared with the experimental data of Begent and Born (1).

Simulations were extended to investigate the effect of pulsatility of blood flow. The inflow was prescribed to have a steady component and a simple harmonic component, the amplitude of the fluctuating component being  $\varepsilon$  times the steady component, with values of  $\varepsilon$  ranging from 0.1 to 0.7. The frequency  $\omega$  of the fluctuating component was 1 Hz. The product of the activation delay time  $\tau$  and the frequency  $\omega$  is a dimensionless parameter. Both might be modified pharmacologically and largely independently, so behavior of thrombus growth at other values of the product are prospectively interesting to determine whether there are zones of behavior worth targeting and reasons for possible differences in thrombus growth between small animal (higher  $\omega$ ) and large animal (lower  $\omega$ ) observations, while  $\tau$  differs less between the relevant species.

## Biological Model

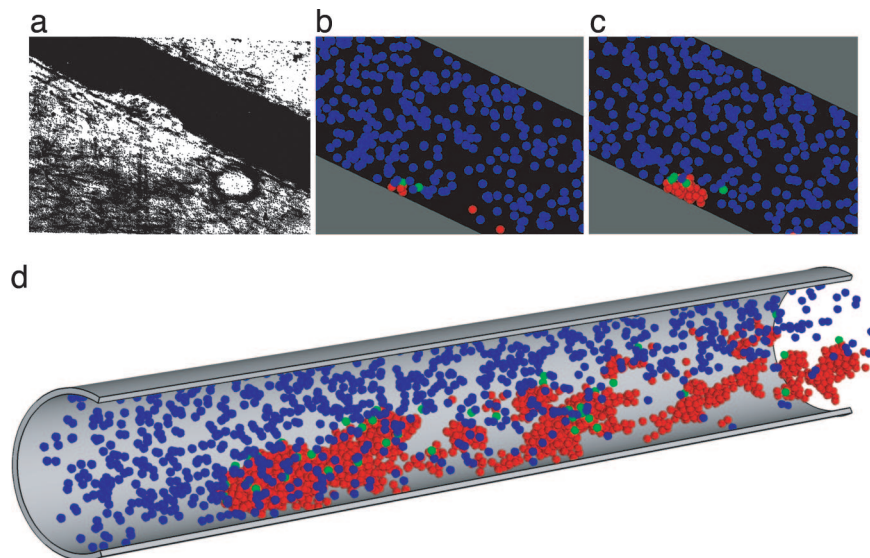
With the mode of supply of ADP used by Begent and Born (1), one can expect that there is a period in which the concentration of ADP builds up parallel to the axis of the blood vessel, and therefore the axial location at which the ADP concentration caused by the iontophoresis is large enough to initiate activation of platelets advances upstream for a while. The footprint of ADP concentration around the outside of the vessels Begent and Born used was likely

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**Fig. 1.** Evolution of thrombus growth. (a) Thrombus growing on a blood vessel wall *in vivo* is shown. [Reproduced with permission from ref. 1 (Copyright 1970, Nature Publishing Group).] (b) Similarly scaled computer model showing the early growth stage of thrombus is shown. Blue indicates unactivated platelets, green indicates triggered platelets, and conversion after a characteristic time delay to activated is indicated by red. (c) Later stage in thrombus growth at steady flow is shown. (d) Shown is a late stage in a similar computation, where adhesion of activated platelets is allowed at all locations downstream.

to have an elliptic form progressively “wrapping around” the side of the vessel close to the iontophoresis needle tip and changing in its axial- and circumferential-direction spans for some time. In the experiments, the size of this footprint likely increased progressively with time.

In the simulation approach, it has been important to explore a selection of rules applied for every platelet regarding the inter-platelet and platelet–wall interactions. Thrombi, except those plugging a vessel wall puncture, have a degree of loose-packing compared with, say, sedimentary behavior of solid grains packing with solid-surface contact. Fibrinogen and fibrin strands have a part of this process and were recognized early as essential cofactors in aggregation; platelet “stickiness” develops when the platelet membrane acquires the ability to bind fibrinogen (11).

Falati *et al.* (12) used confocal and wide field microscopy to image thrombus formation with platelets, fibrin, and tissue factor in real time. Vessel wall injury was induced by a pulsed nitrogen dye laser (nonpuncture injury). Platelets were visible in attachment by 4 s after injury. Polanowska-Grabowska and Gear (13) had shown that platelets can adhere very rapidly to collagen exposed on a surface. Falati *et al.* (12) found colocalization of the platelets and the fibrin in the thrombus. Tissue factor was localized on the upstream edge of the thrombus and along the vessel–wall interface. Falati *et al.* (14) later provided additional information on tissue factor accumulation in developing thrombi. Plasma fibronectin is also known to have a role in thrombus growth and stability (15).

Activation of platelets initiated by ADP can occur at a finite distance of separation from a growing thrombus for platelets approaching it, because of diffusion of ADP from the thrombus (or from an extravascular iontophoretic source). These aspects of platelet interaction invoke use of two length scales. Another issue for incorporation in an interaction model is that of a repulsive force function in the event of close approach. Energy landscapes have been described for single molecular bonds (16), which can be studied under ingeniously designed and carefully controlled laboratory conditions that assure single bonds only are involved. Thrombi develop *in vivo* with multiple bonds, and so a more generalized form of energy landscape is applied for the calculations reported here. The links used in the model here incorporate the effects of many individual bonds.

One extra choice available is that for the adhesive footprint of the thrombus on the wall to which it attaches: given a seeded location (where a few platelets are adherent, a computational-model replacement of the use of iontophoretic application of ADP to initiate

thrombosis), should any activated platelet be allowed to attach anywhere it comes sufficiently close to the wall surface downstream? Or should a geometrically defined patch on the wall limit the extent where that may happen? Our simulations reported here cover these two cases. A range of choice of footprint rules for the computation may be needed to represent adequately typical different causes of thrombus formation, such as highly localized vascular injury, or fissures at atherosclerotic plaque caps, or flow over manufactured surfaces as in needles or over artificial-organ components. Even within one footprint type, there can be an effect of the relative locations of the small number of seed platelets present at the beginning, which also has been explored somewhat.

## Results

The simulation predicts thrombi growth with shapes and patterns similar to those observed experimentally. Fig. 1 shows one frame from the results of Begent and Born (1) and a pair of frames from a simulation of such a thrombus growth (see also Movie 1, which is published as supporting information on the PNAS web site). There is an early, brief (up to  $\approx 3$  s) phase of rapid growth, which would not have been detected in Begent and Born’s experiments because of the difficulty of seeing distinctly a mural grouping of so few platelets, followed by a slower yet exponential rate of growth.

Thrombi initiated under the same flow conditions may have a varied small-growth time, but have major growth at an exponential rate that has no set relation to variation in the small-growth time, and embolization of part of a thrombus can readily resolved in the computation even for thrombi as small as 10 platelets.

The number of platelets accumulated in a thrombus for replicate computing runs at one flow velocity is shown in Fig. 2*a*. The lines correlating each run in the exponential-growth phase have closely similar slopes, and the time taken to that phase from the initiation of flow varies somewhat. This result is similar to that reported by Begent and Born (1), except that they had no way for observing the variation of the short initial phase because the number of platelets adhering to the wall then was too small, being below the resolving power of their microscope, nor did they run a number of replicate runs at each flow rate to determine statistics of the variability of the growth-rate factor as a function of blood flow rate. The slope of the exponential growth for the model was calculated as a mean and standard variation from the replicate runs.

The model used provides for flow-structure interaction, as illustrated in Fig. 2*b*. Fig. 2*b* displays, in 3D at one instant in time, some flow lines computed at locations lying closely over a thrombus in an early stage of its growth. The streamlines, of which a small







conditional aspects the model is intended to make practical allowances for physico-physiological aspects in ways that avoid requirement of concurrent solutions for e.g., time-dependent ADP transport to be generated as these would be computationally prohibitive at the present time. Much detailed biochemistry is condensed, and only the associated major changes in physical forces are modeled here. The model is chosen to allow computations to march forward in time, without iteration. Each time a computation is performed with constant values of parameters and the same flow rate, there is some variation from the results of otherwise similar runs when the random-number generator for determining individual platelet activation delay times is freshly seeded. Thus, replication runs are made to explore the corresponding variability of thrombus growth.

The governing flow equations are solved by using the spectral/hp element solver NEKTAR (23) marching forward in time steps, the position vectors for all of the platelets being updated (and all associated near-neighbor conditions being checked) for each time step. The force coupling method seems more reliable when the average particle density is modest, and so the suspension of red cells is treated as a continuum. The impact of this assumption is believed to be small because the Smoluchowski number, ratio of shear gradient encounter rate to random-walk collision rate, for platelets in the flow considered here is quite high, and an augmentation of platelet diffusivity would not have a significant effect. We focus on the onset of the aggregation and consider small aggregates of size  $\approx 100 \mu\text{m}$ . For aggregates of this size the increase of platelet near-wall concentration caused by the presence of the red blood cells should have minor effects on the results obtained here (24). The few other cells typical of whole blood such as the leukocytes are omitted from the model as being too low in number density to have a significant dynamic effect. Even so, using this model has consumed significant amounts of supercomputer time (hundreds of thousands of hours) over a period of 2 years, including sensitivity studies.

At the beginning of the computation, the fluid in the vessel is empty of platelets but the entering flow has them approximately uniformly distributed in it. However, by the time there are platelets sufficiently close to the seed platelets on the vessel wall to be activated, there is full priming of the flow at smaller radii with platelet-laden blood. To initiate thrombus growth at a known location, typically three activated platelets were placed close together on the vessel wall at the initiation of flow. (In pulsatile flows of large amplitude, these were observed to oscillate somewhat back and forth in the flow direction, a natural consequence of the model and sometimes seen in actual flows.) Approaching platelets, which come close enough to these, become triggered; while a few triggered platelets escape downstream, many become activated while still close enough to adhere, and through continuous repetition of this process the platelets aggregate as a mural thrombus.

Interaction potentials applied with soft matter are typically quadratic. Hence, our interaction force term ( $F_{\text{interaction}} = F_1 + F_2 + F_3 + F_4$ ) is piecewise linear, the part for closer approach having

the repulsion force rising linearly with decreasing distance. Specifically, the force acting on the platelet approaching the wall or another platelet is

$$F_1(r) = 2\alpha \left(1 - \frac{r/a}{R}\right)$$

for  $r/a \leq R$ , where  $a$  is the platelet radius and  $r$  is a distance from the center of the platelet to the wall or the surface of the other platelet. The force is directed along the normal to the wall or the vector connecting the centers of the platelets. From the distance at which that has become zero, a region of zero force is applied,  $F_2(r) = 0$  for  $R \leq r/a \leq L$  (representing where connecting proteins, especially fibrin, may be slack), beyond which an attractive force rises linearly with increasing distance,

$$F_3(r) = \alpha \left(\frac{r/a}{L} - 1\right)$$

for  $L \leq r/a \leq M$ , representing a combination of connecting protein/filopodia and cell membrane elasticity. The force between activated platelets rises up to a point where typically the connections are not long enough to reach, or have broken from, the neighbor platelet, with the force dropping to zero at an out-of-range position,

$$F_4(r) = \alpha \left(\frac{M}{L} - 1\right) \frac{B - r/a}{B - M}$$

for  $M \leq r/a \leq B$ . The attraction force is directed along the vector between the center of the platelet and the attachment point on the wall or the center of another platelet. The values of parameter  $R$ ,  $L$ , and  $B$  are set to 1, 1.5, and 3.5, respectively, while

$$M = \frac{L + B}{2};$$

the constant  $\alpha$  is set to  $4 \times 10^{-9} N$ . These parameters were chosen based on physical considerations and systematic simulations to evaluate the sensitivities of the model. For example, we have performed 36 simulations for three different values of  $\alpha$  corresponding to  $\times 1/10$ ,  $\times 1/3$ , and  $\times 3$  the above value (at flow rate  $400 \mu\text{m/s}$ ), and all results were within the range established by the value of  $\alpha = 4 \times 10^{-9} N$  at the same flow rate. Finally, the activation delay time is assumed randomly uniformly distributed over the range 0.1 to 0.2 s, selected for each platelet once, but differently in otherwise replicate runs. The platelet recovery time is set to 5 s (5).

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